

Infrared Optical Systems

OPTI 696

Practical Optics Seminar

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Raytheon Missile Systems

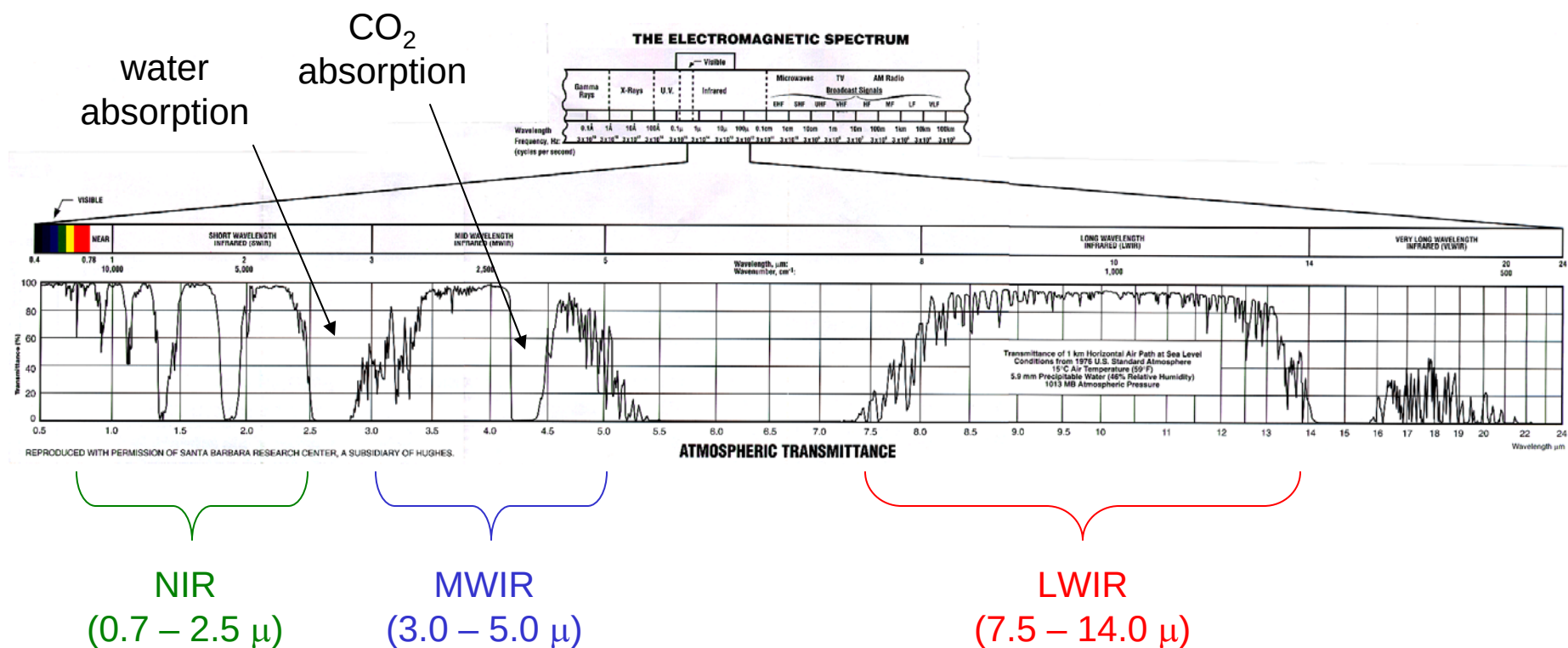
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Atmospheric Transmittance



Blackbody Radiation

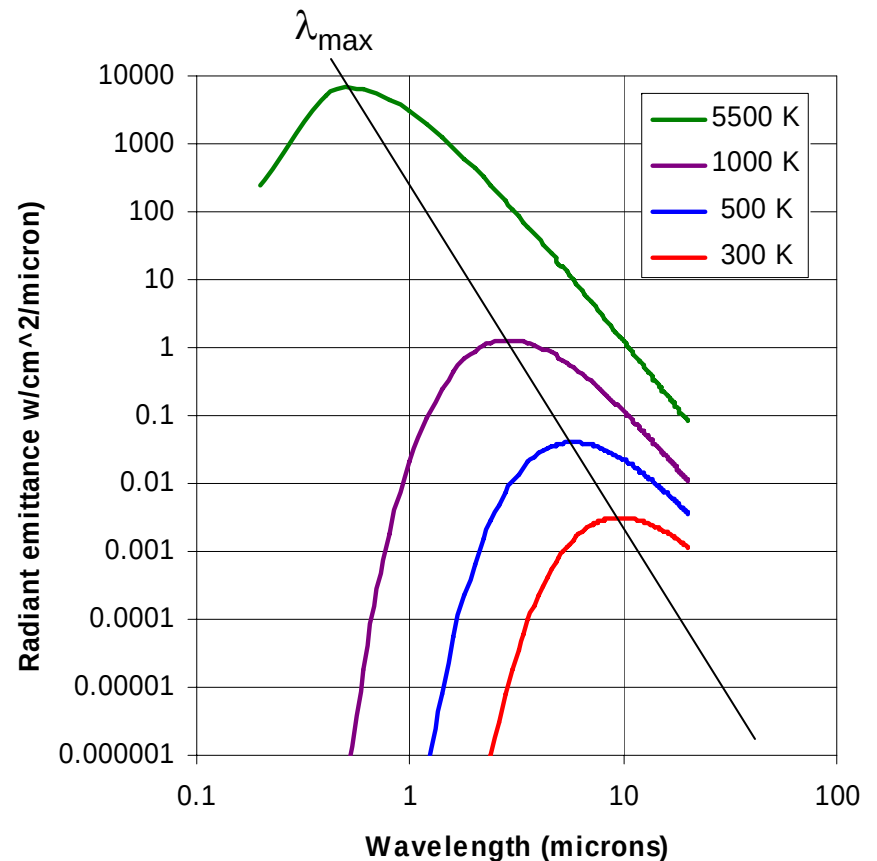
- Blackbodies emit per the following equation

$$W(\lambda) = \frac{c_1}{\lambda^5 (e^{c_2/\lambda T} - 1)}$$

$$c_1 = 2\pi c^2 h = 37418.32 \text{ W}\mu^4\text{cm}^{-2}$$

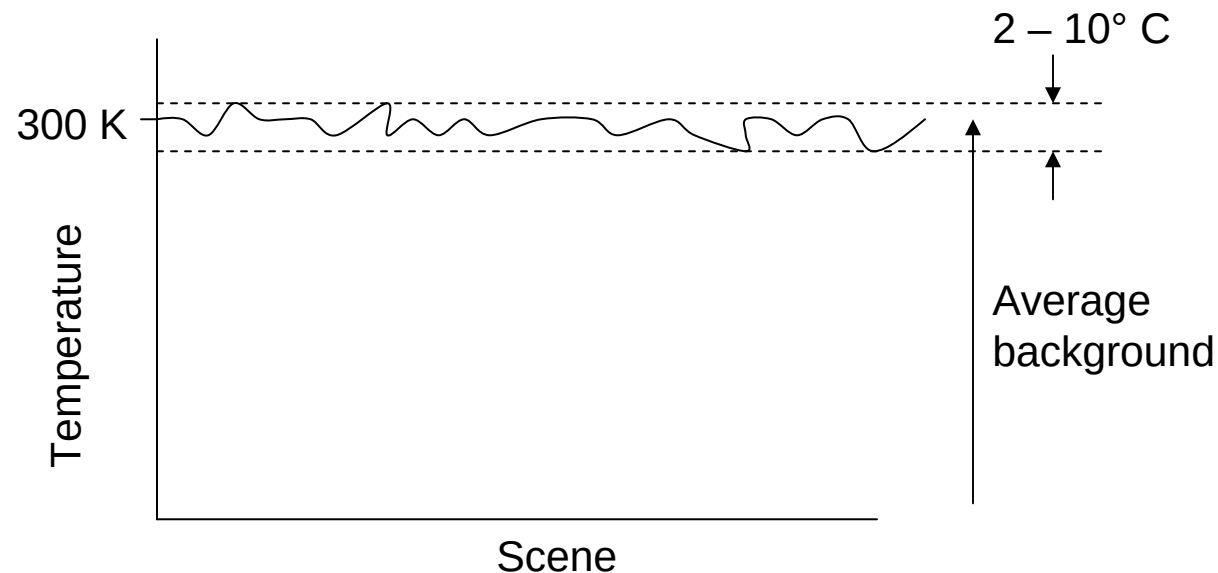
$$c_2 = hc/k = 14387.86 \mu\text{K}$$

- The peak of the curve occurs at
 $\lambda_{\text{max}} = 2898/T$
 - Visible (T = 5500) $\lambda_{\text{max}} = 0.53 \mu$
 - MWIR (T = 500) $\lambda_{\text{max}} = 5.8 \mu$
 - LWIR (T = 300) $\lambda_{\text{max}} = 9.7 \mu$
- The choice of spectral band to use depends on the temperature of the object you want to detect



Thermal Contrast

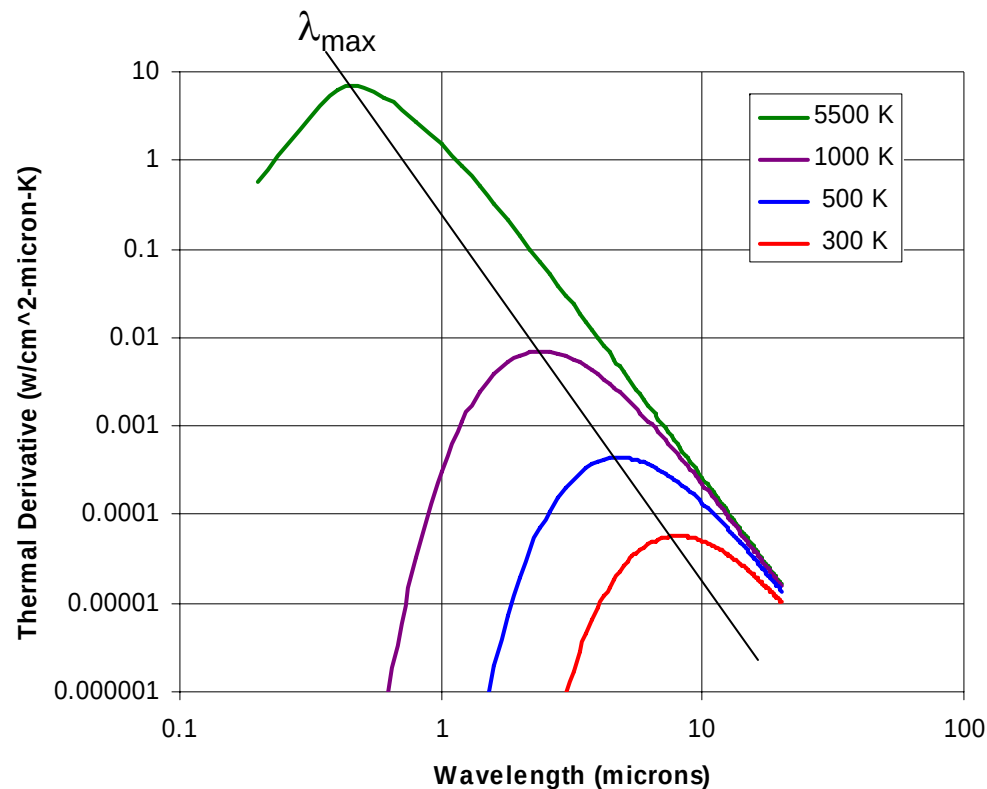
- Terrestrial objects are at about 300 K ($\sim 25^\circ\text{C}$)
 - The human body, for example, has a thermal contrast of about $3 - 8^\circ\text{C}$
- Thus, a typical IR scene has a contrast of only a few percent (as opposed to visible scenes, which have 100% contrast)
- To maintain the dynamic range in the important part of the image, the background is usually subtracted out



Blackbody Thermal Derivative

- Since the background is subtracted from the IR scene, the sensor really detects the change in temperature, or the thermal derivative $\partial W / \partial T$

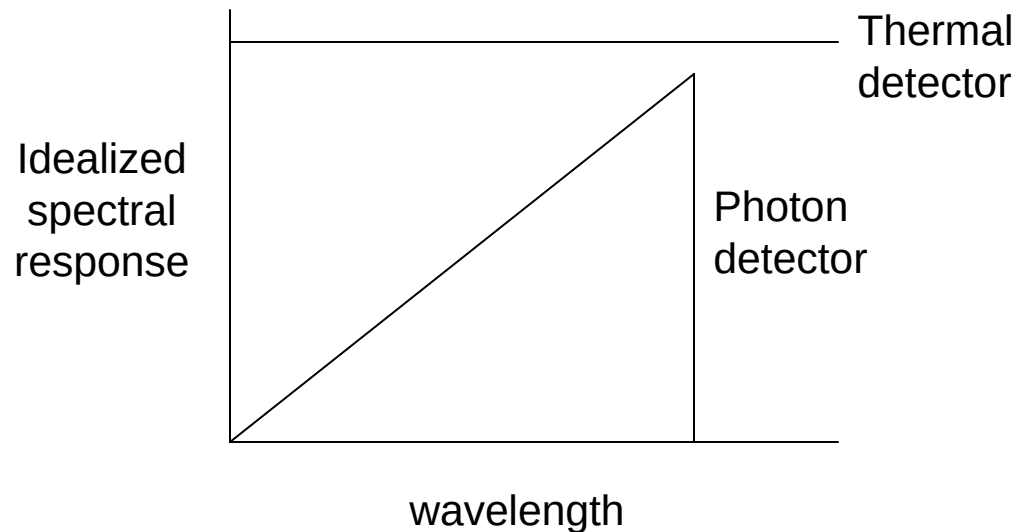
$$\frac{\partial W}{\partial T} = \frac{c_1 c_2 e^{c_2/\lambda T}}{\lambda^6 T^2 (e^{c_2/\lambda T} - 1)^2}$$



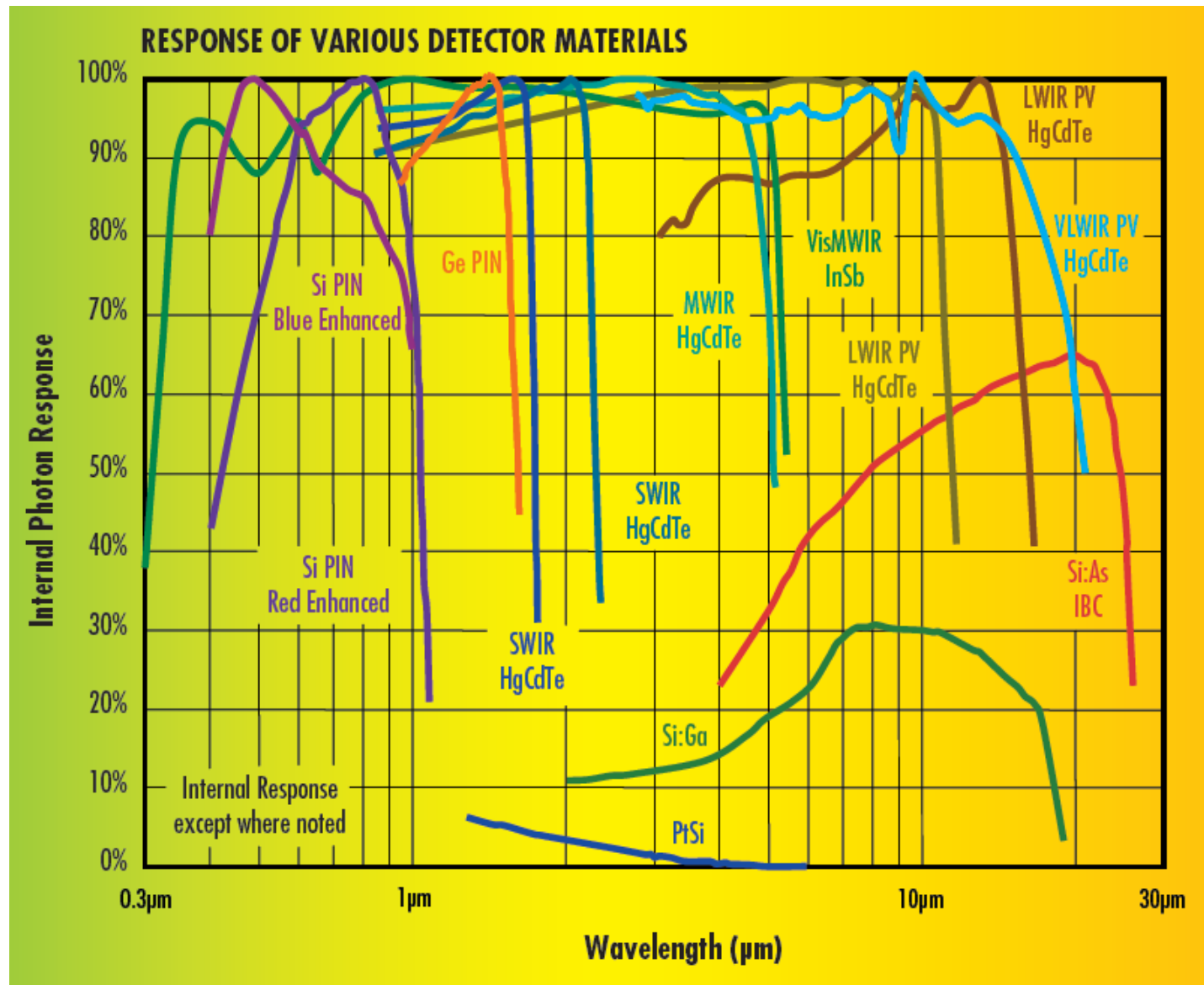
Peak wavelength
is at $\lambda_{\max} = 2410/T$

IR Detectors

- Two kinds of IR detectors
 - Thermal detectors – sense temperature
 - Photon detectors – sense photon energies
- Thermal detectors have a flat spectral response with wavelength
- Photon detectors have a spectral response proportional to wavelength with a peak wavelength (related to material properties such as band gaps) beyond which there is little or no response



Infrared Detectors



IR Signal

- The total signal received by the detectors is the product of the target spectral emission, the atmospheric transmittance, the optical transmittance, and the detector spectral response

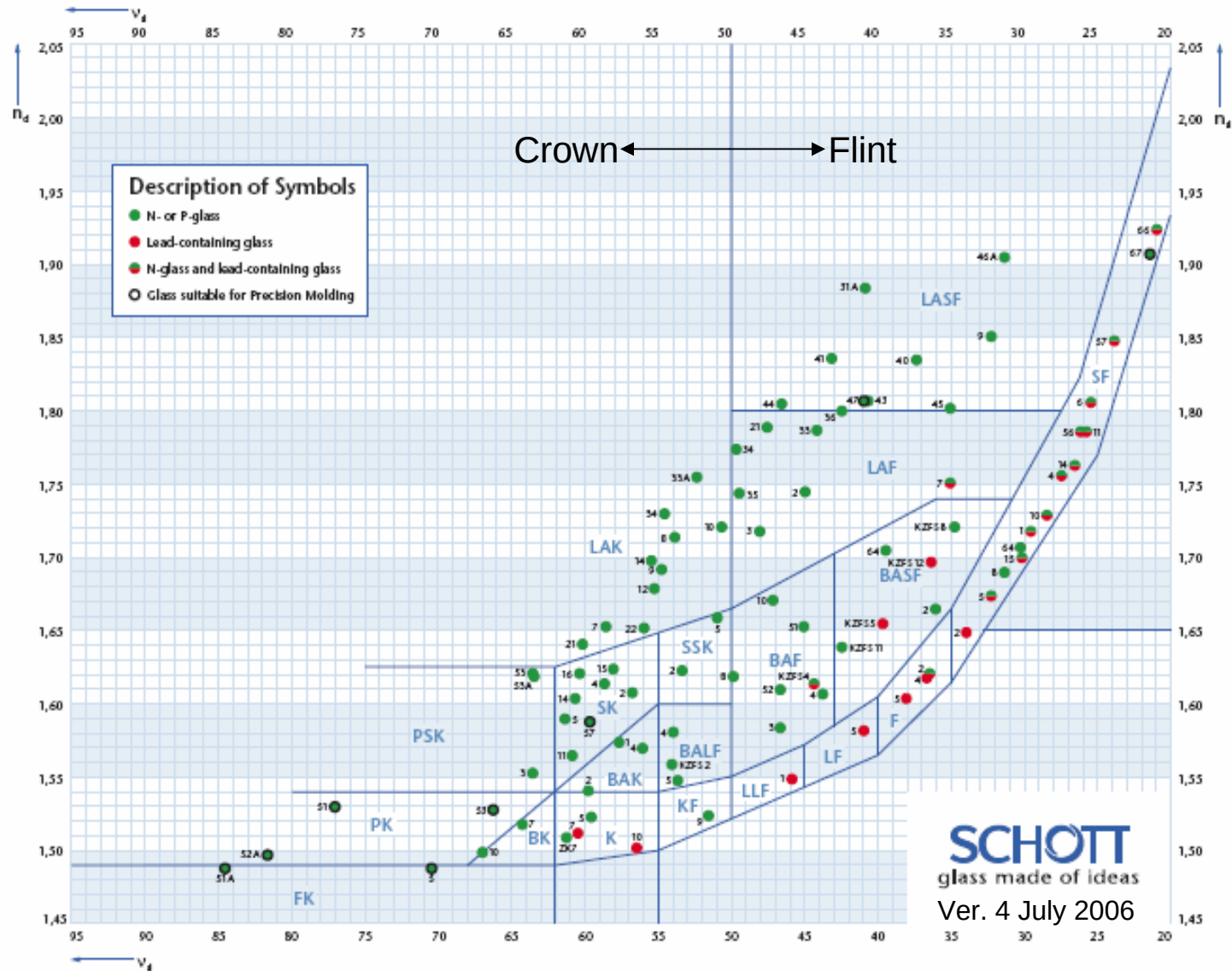
$$\text{Signal} = \int E_{\text{target}}(\lambda) \tau_{\text{atmosphere}}(\lambda) \tau_{\text{optics}}(\lambda) R_{\text{detector}}(\lambda) d\lambda$$

- Of course, there's also the radiometric factors such as target size, solid angles, f/numbers, detector size, etc., which we will not go into here
- We are also ignoring for this seminar the noise contributions such as thermal background, detector noise, electronic noise, etc.

Infrared Glasses vs. Visible Glasses

- IR glasses have significantly higher refractive indices
 - Visible glass – n ranges between 1.45 and 2.0
 - IR glasses – n ranges between 1.38 to 4.0
- Dispersion can be significantly lower (depending on spectral band)
 - Visible glasses – V ranges from 20 to 80
 - IR glasses – V ranges from 20 to 1000
- Many IR glasses are opaque in the visible
 - And most visible glasses are opaque in the IR
- IR glasses are often heavier than visible glasses
- IR glasses have significantly higher dn/dT values (factor of 10 or more higher)
- IR glasses cost more than visible glasses (by 2 or more orders of magnitude)
- Significantly fewer number of practical IR glasses than visible glasses

Visible Glass Map



Infrared Glasses

- The list of commonly used IR materials is (unfortunately) pretty short

Germanium

Silicon

Zinc Sulfide

AMTIR 1, 3

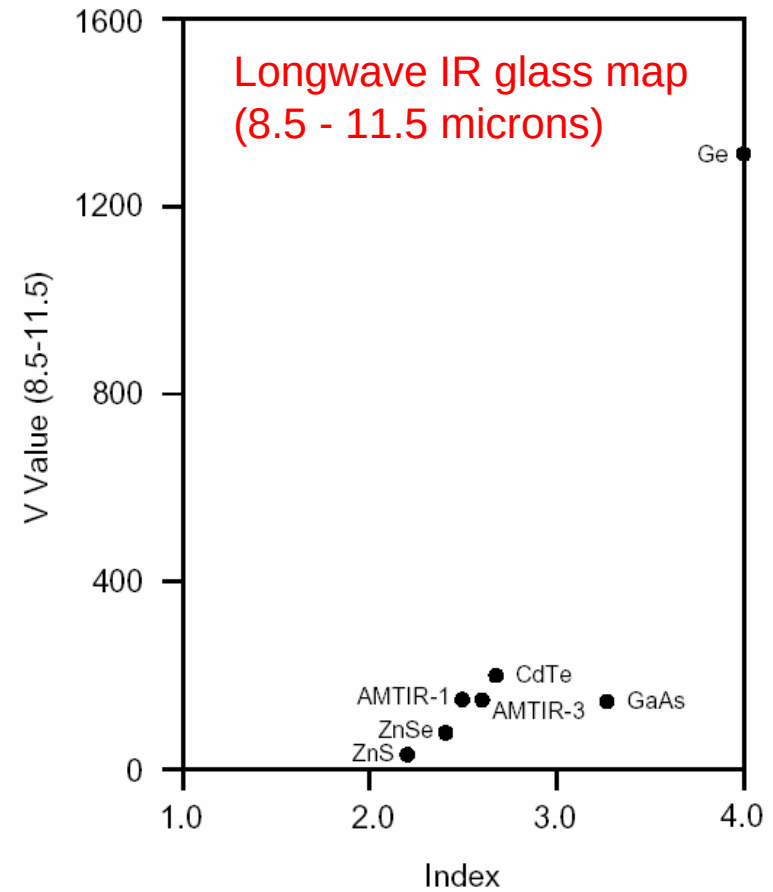
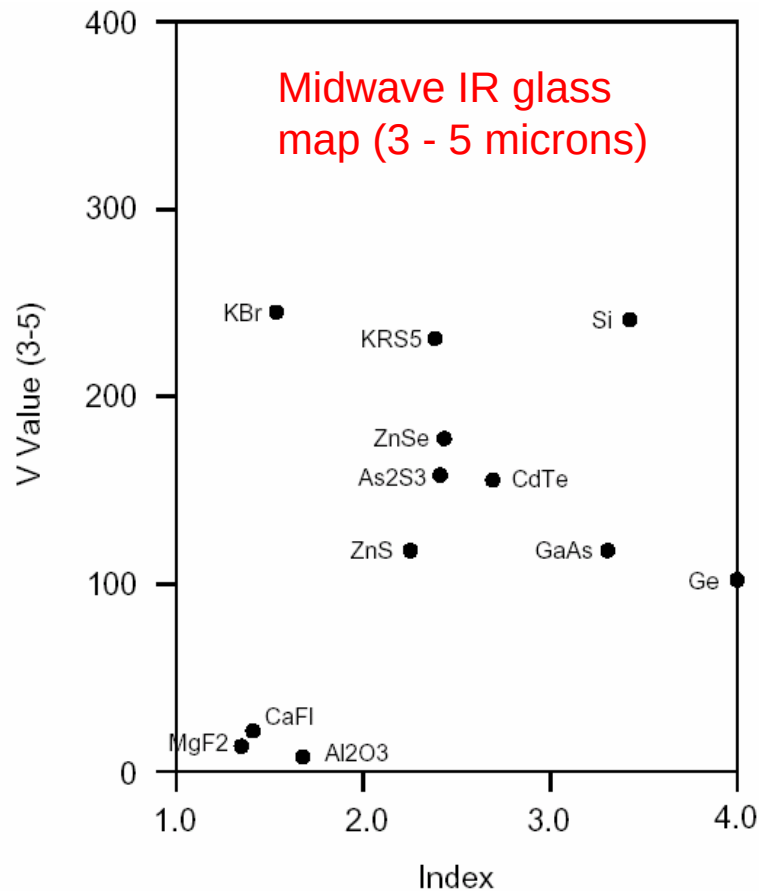
Sapphire

Zinc Selenide

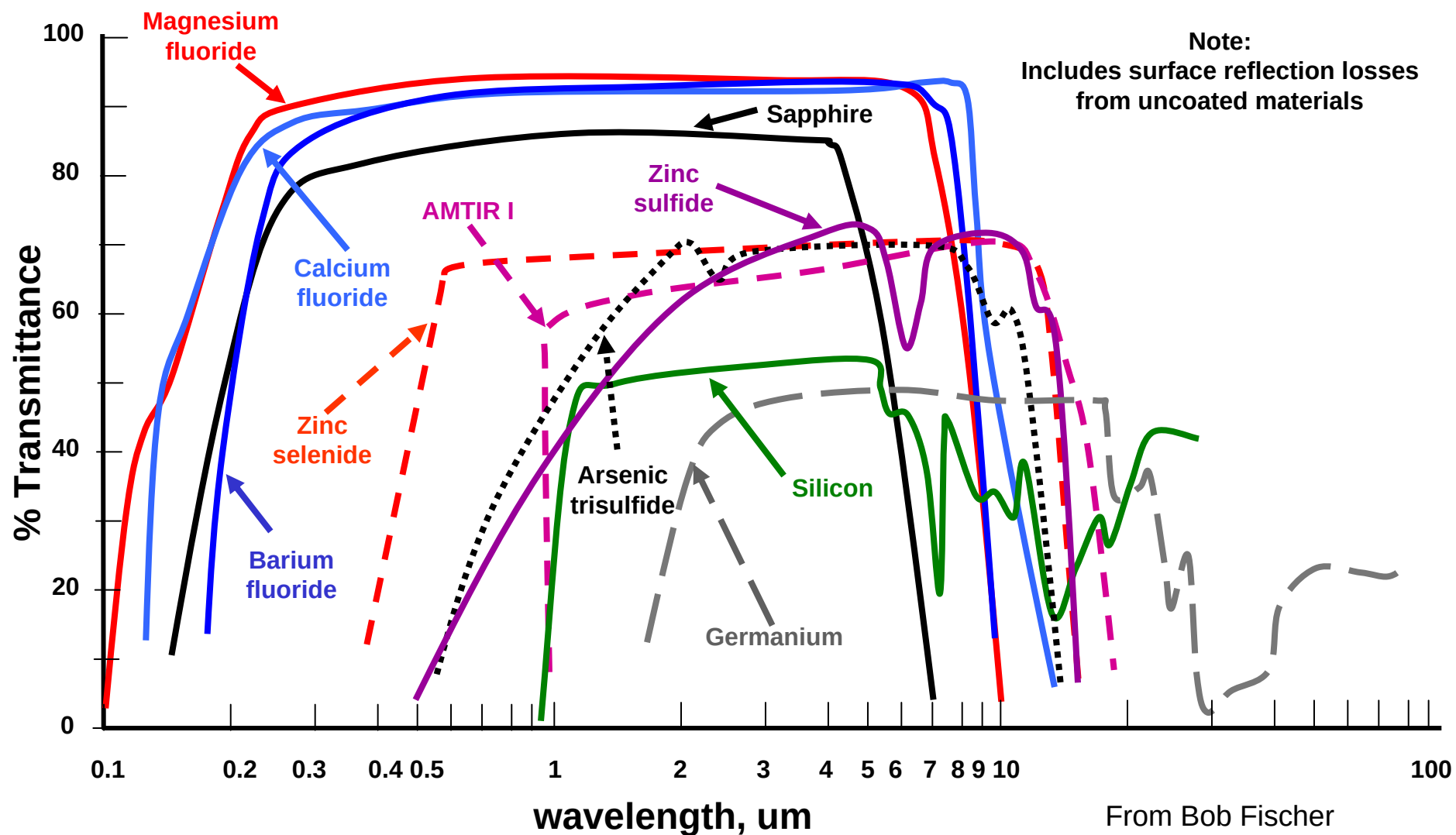
Magnesium Fluoride

Gallium Arsenide

Calcium Fluoride



Transmittance of IR glasses



Designing With IR Glasses

- Advantages 😊

- Refractive index is usually higher, so fewer lenses are needed to achieve diffraction-limited performance
- Dispersion is often low enough such that color correction may not be necessary
- Most IR materials can be diamond point machined, so aspherics are commonly used in designs
- The Airy disk size and diffraction-limited depth of focus are larger for the IR than for the visible, so achieving diffraction-limited performance is easier

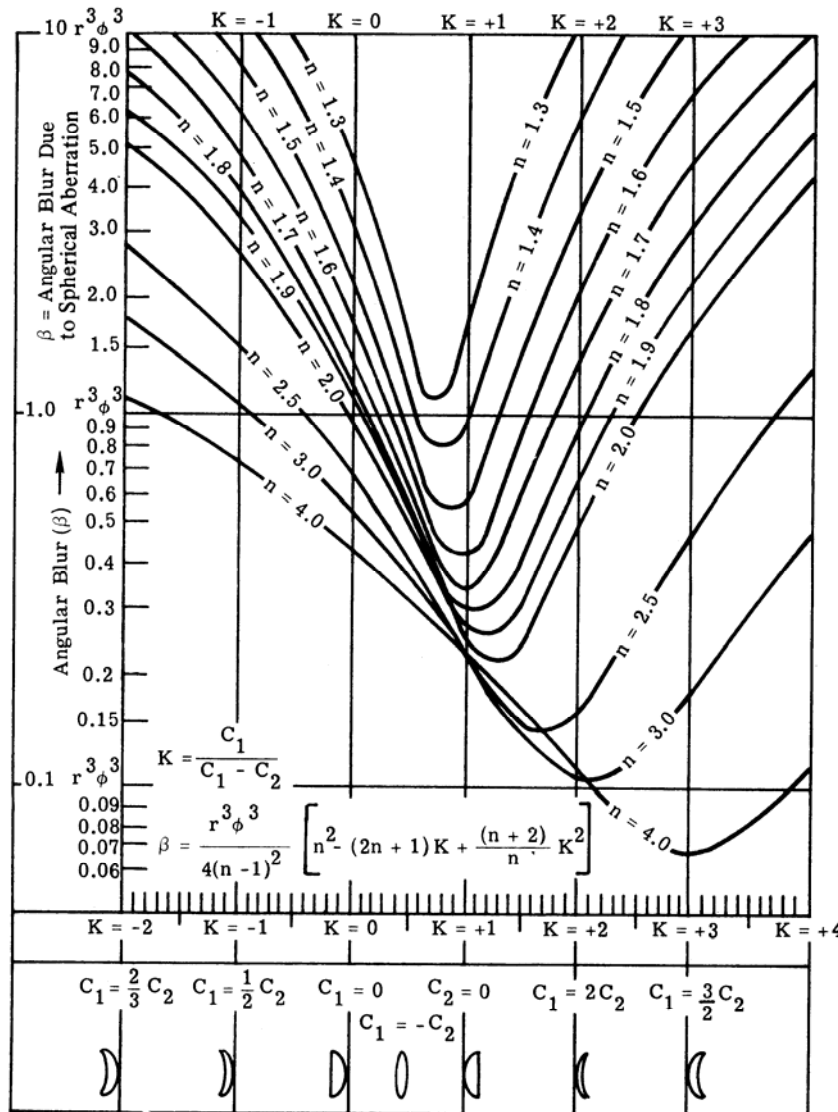
- Disadvantages ☹

- Small choice of glasses
- Materials are expensive (~1\$/gram)
 - One-inch diameter BK7 lens \$5
 - One-inch diameter germanium lens \$500
 - Five-inch diameter sapphire dome Priceless
- Some IR materials are difficult to fabricate and/or antireflection coat
 - Fragile, soft, chip easily, low thermal conductivity, etc.
- Most IR materials have large dn/dT values, so athermalizing can be difficult

Cautions on IR Glasses and Optics Software

- There is only one source of data on Schott glasses – Schott Optical Glass
- However, there is no "source" of data on IR glasses
- Most optical software programs depend on some literature source of data for IR materials, then fit the data to Sellmeier equations
 - Some programs do a better job of this than others
- Some IR glasses, such as AMTIR, are made by a specific supplier who publishes index data on the material
 - Sometimes these data are not consistent, come from different measurement sources, and may not have sufficient significant digits
 - In these cases, if your design is sensitive to the glass dispersion, you may need to double-check the index data
- Thermal data, such as thermal expansion coefficient and dn/dT data may vary widely for some materials, depending on who measured it
 - Usually, optical software do not include these data, as there is no official "source" for these data

Spherical Aberration vs. Refractive Index



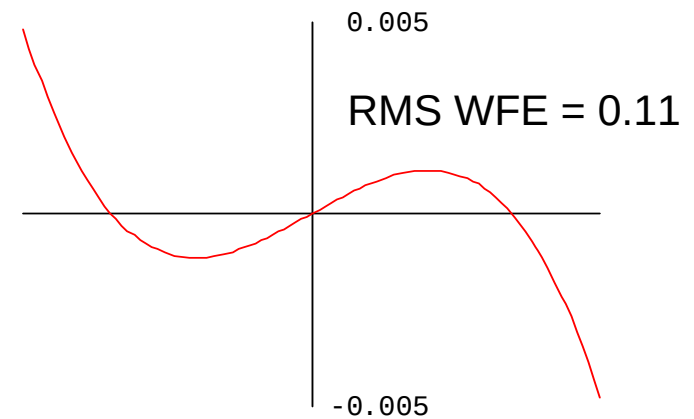
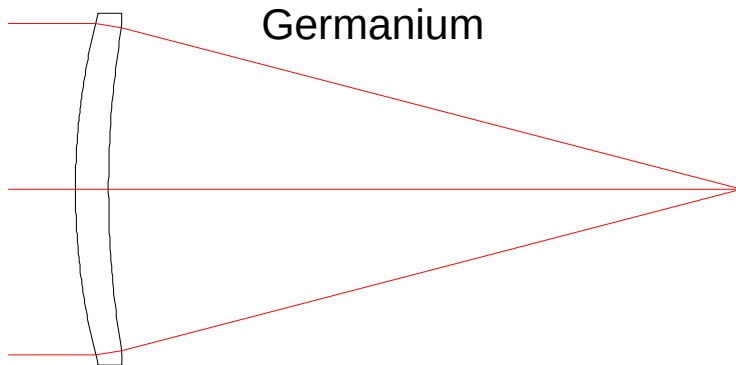
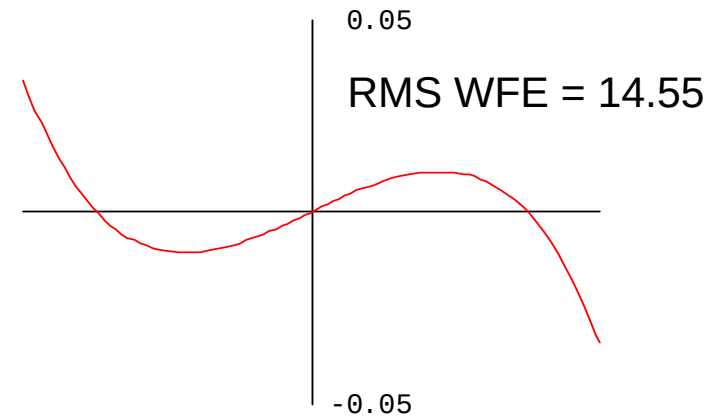
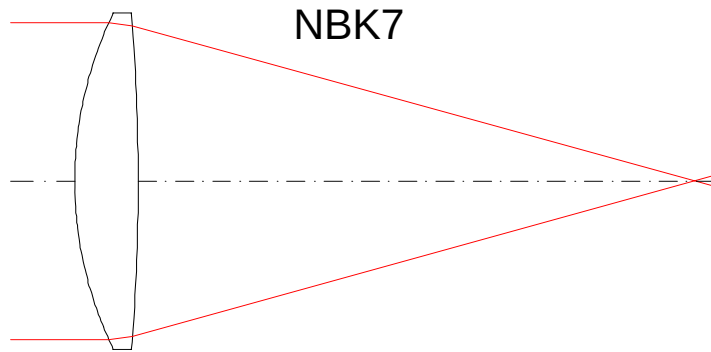
$$K_{\min} = \frac{n(2n+1)}{2(n+2)}$$

$$\beta \text{ at } K_{\min} = r^3 \phi^3 \frac{4n^2 - n}{16(n-1)^2(n+2)}$$

For germanium $n = 4$

$$\beta = \frac{0.0087}{f^3}$$

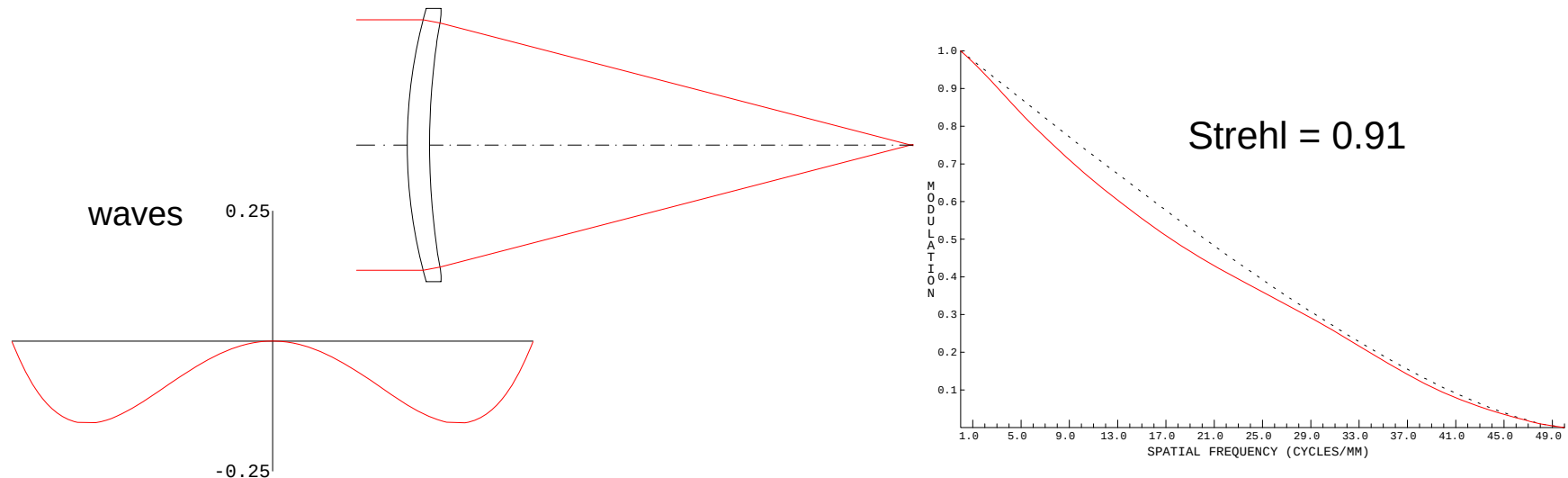
NBK7 vs. Germanium – Spherical Aberration



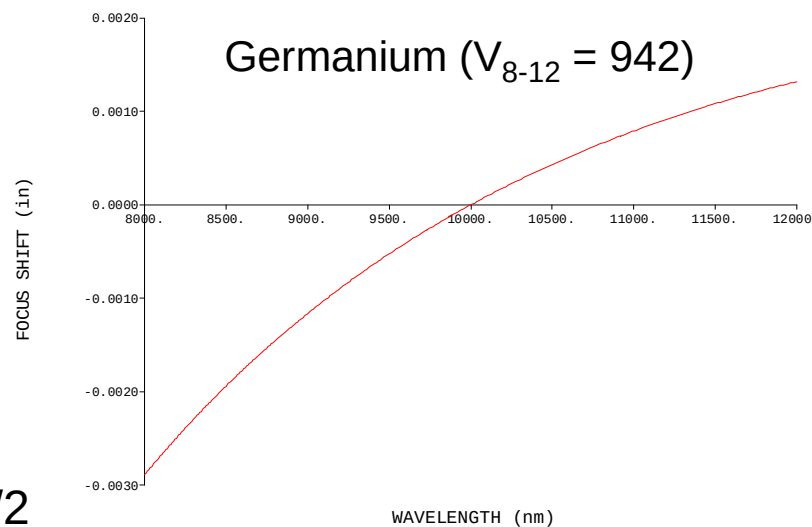
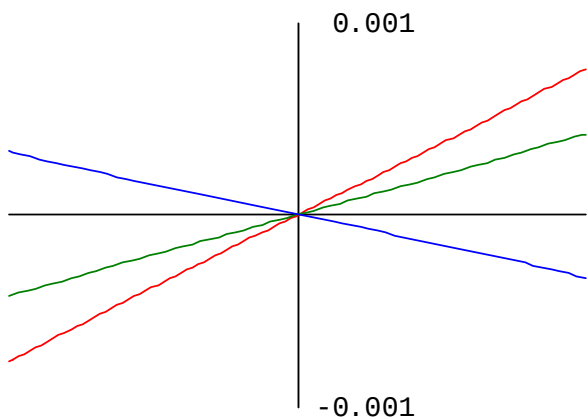
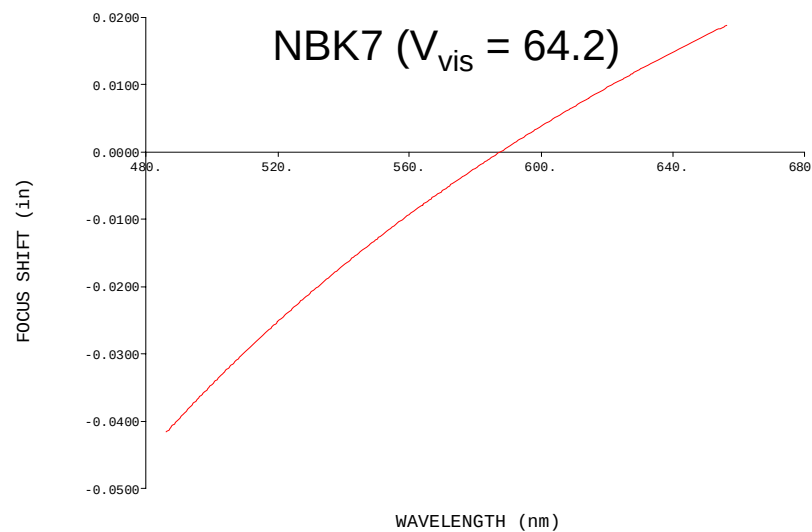
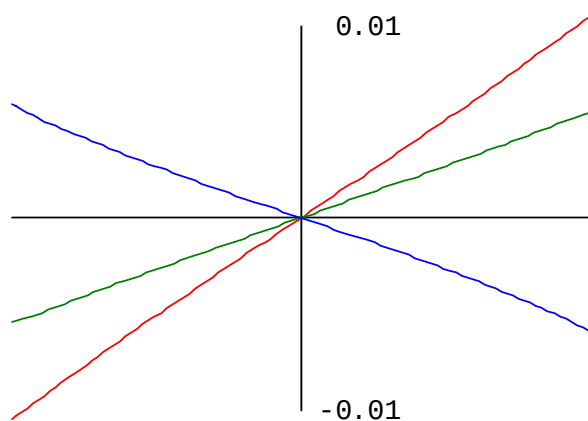
4.0 inch EFL, f/2

Example - Germanium Singlet

- We want an f/2 germanium singlet to be used at 10 microns (0.01 mm)
- Question - What is the longest focal length we can have and not need aspherics to correct spherical aberration?
- Answer
 - Diffraction Airy disk angular size is $\beta_{\text{diff}} = 2.44 \lambda / D$
 - Spherical aberration angular blur is $\beta_{\text{sa}} = 0.0087 / f^3$
 - Equating these gives $D = 2.44 \lambda f^3 / 0.0087 = 22.4 \text{ mm}$
 - For f/2, this gives $F = 45 \text{ mm}$



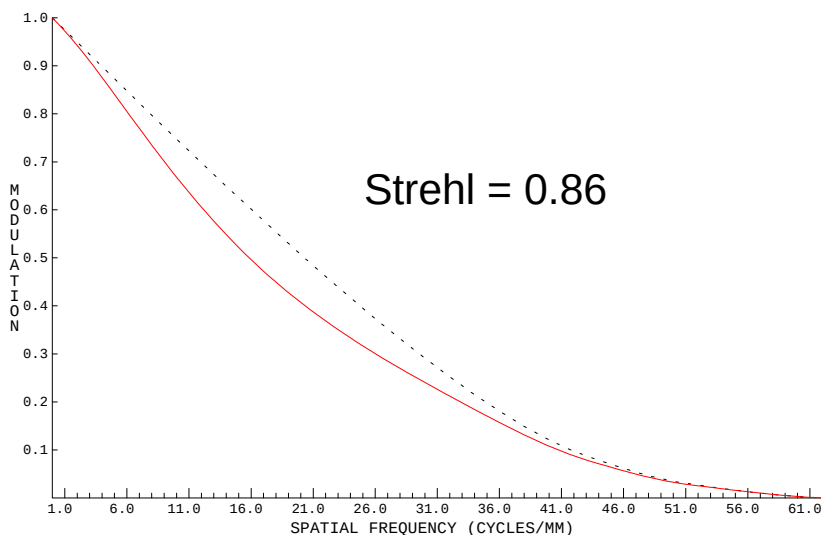
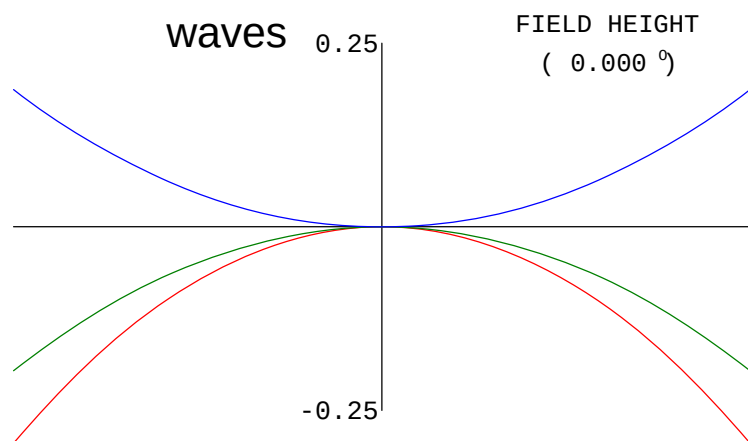
NBK7 vs. Germanium – Chromatic Aberration



4.0 inch EFL, f/2

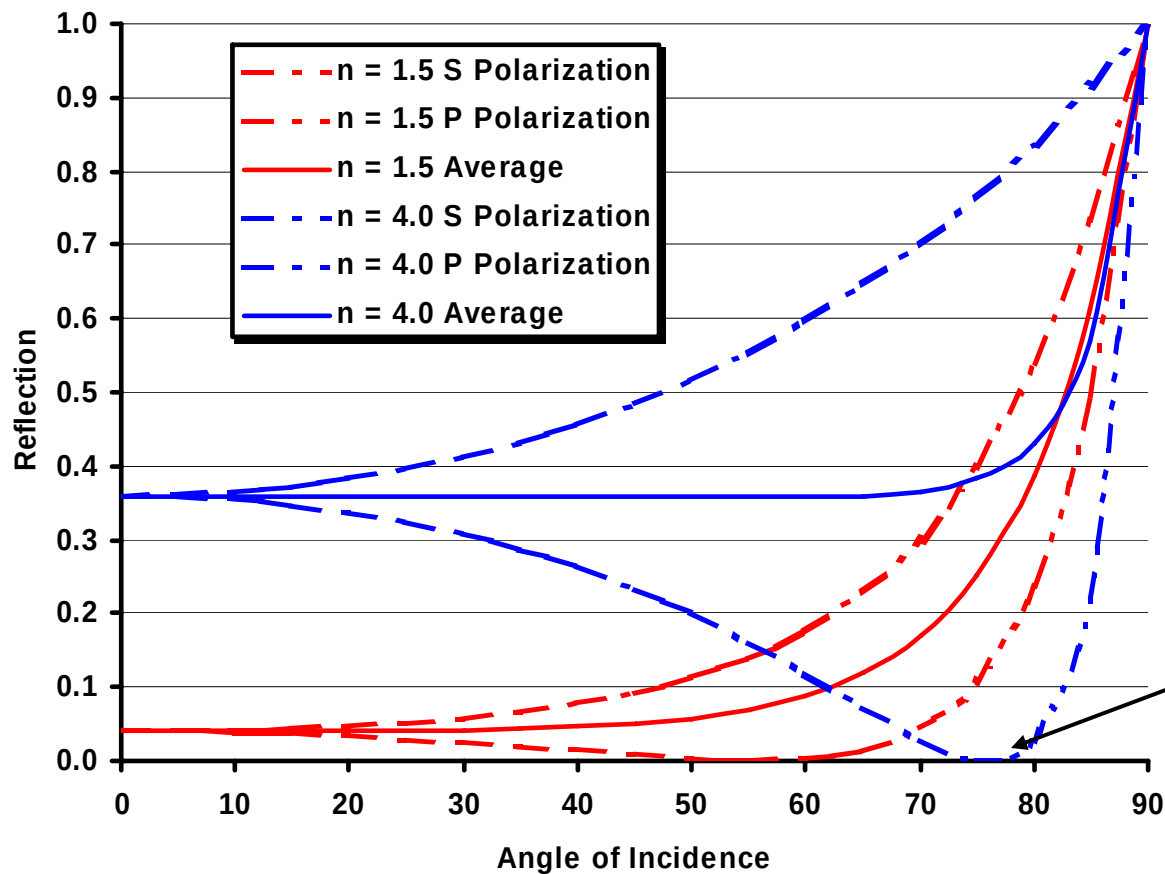
Chromatic Aberration Example - Germanium Singlet

- We want to use an f/2 germanium singlet over the 8 to 12 micron band
- Question - What is the longest focal length we can have and not need to color correct? (assume an aspheric to correct any spherical aberration)
- Answer
 - Over the 8-12 micron band, for germanium $V = 942$
 - The longitudinal defocus = $F / V = F / 942$
 - The 1/4 wave depth of focus is $\pm 2\lambda f^2$
 - Equating these and solving gives $F = 4 \cdot 942 \cdot \lambda \cdot f^2 = 150 \text{ mm}$



Surface Reflection

- Bare glass reflects a portion of the light hitting it
 - The amount reflected depends on the index of the glass, the angle of incidence of the light, and the polarization of the light



$$R_S = \frac{\sin^2(\theta - \theta')}{\sin^2(\theta + \theta')}$$

$$R_P = \frac{\tan^2(\theta - \theta')}{\tan^2(\theta + \theta')}$$

Brewster's
angle = $\tan^{-1}n$

Single Layer Anti-reflection Coating

- The single layer is the simplest anti-reflection (AR) coating
- Let the incident medium be n_0 (usually air, so $n_0 = 1$), the index of the coating be n_1 , and the index of the substrate be n_2
- The reflectivity of the surface for an incident angle θ is

$$R = \frac{r_1^2 + r_2^2 + 2r_1r_2 \cos X}{1 + r_1^2 r_2^2 + 2r_1r_2 \cos X} \quad \text{where} \quad X = \frac{4\pi n_1 t \cos \theta}{\lambda}$$

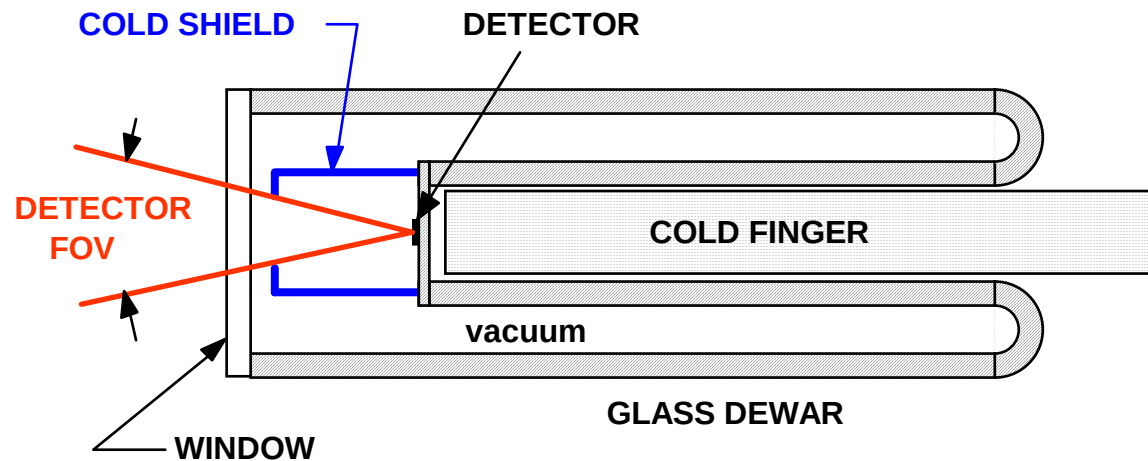
– R is minimized when $\cos X = -1$, or when $n_1 t = \lambda/4$

- For normal incidence, $r_1 = \frac{n_0 - n_1}{n_0 + n_1}$ $r_2 = \frac{n_1 - n_2}{n_1 + n_2}$

$$\text{Then } R = \left[\frac{n_0 n_2 - n_1^2}{n_0 n_2 + n_1^2} \right]^2 \quad \text{minimized when } n_1 = \sqrt{n_0 n_2}$$

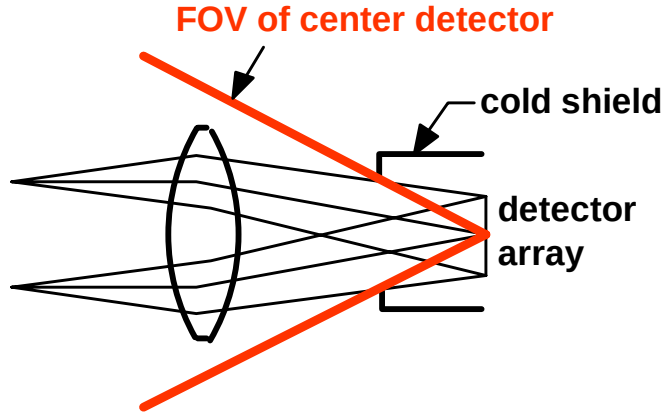
Cooled Detectors

- Many IR systems require a cooled detector
 - Typically cooled to 77 K or lower (liquid nitrogen temperatures)
- To avoid frosting up, the detectors are mounted in a thermally insulated vacuum enclosure called a dewar
- Inside the dewar, a cold shield limits the angle of radiation which can be seen by the detector
 - This increases the detector sensitivity (D^*)

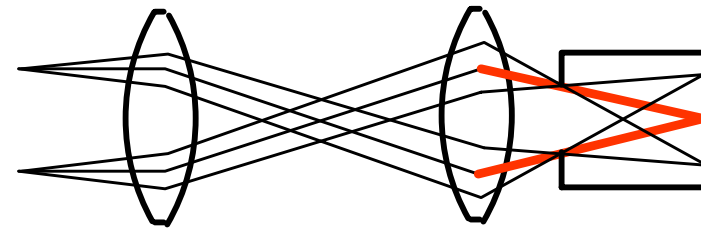


Cold Shield Efficiency

- All IR systems with cooled detectors have a cold shield in the dewar to minimize the background radiation
 - The size of this cold shield determines the amount of background radiation seen by the detector and hence the system sensitivity



**Less than 100% cold shield efficiency
(using simple imager)**

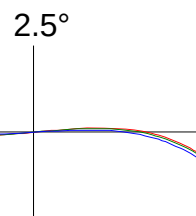
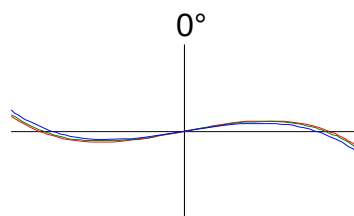
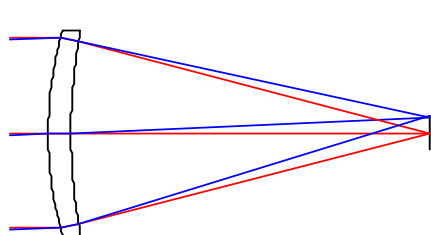


**100% cold shielding efficiency
(using re-imaging imager)**

Aperture Stop and Pupil Aberration

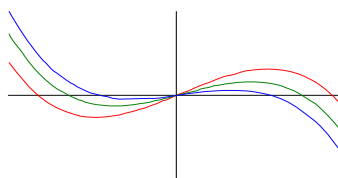
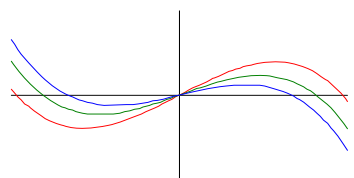
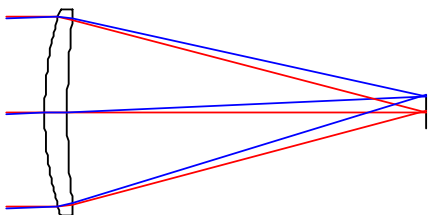
- The aperture stop is usually at one of two locations
 - On the front lens
 - At the cold shield
- Whichever one it is located at, it is often imaged onto the other to minimize its size
- Pupil aberration (spherical or coma of the pupil) usually causes the image of the stop to be oversized by about 10-15%
 - If the stop is at the front objective, this requires an enlarged cold shield
 - Result is lower detector sensitivity and lower system performance
 - If the stop is at the cold shield, this requires an oversized objective
 - This increases cost and weight

Singlet Design Examples – f/2, 50 mm EFL (8 – 12 μ)



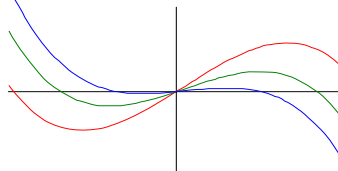
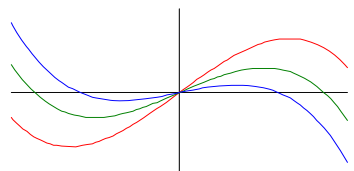
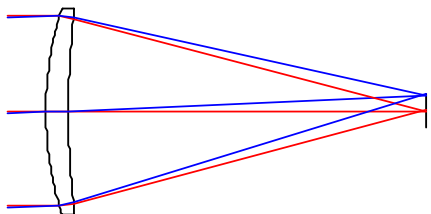
Germanium singlet ($V=942$)

RMS WFE = .096



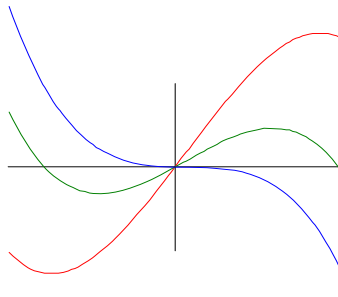
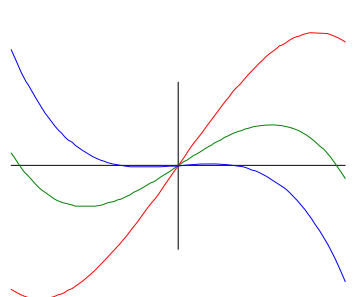
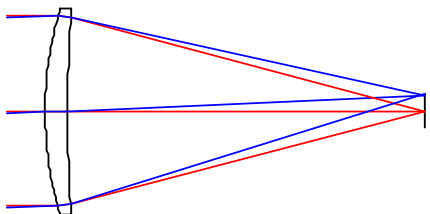
AMTIR-1 singlet ($V = 110$)

RMS WFE = .209



ZnSe singlet ($V = 58$)

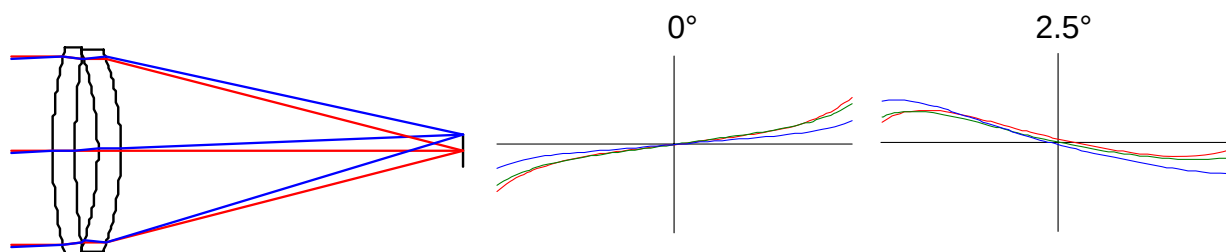
RMS WFE = .331



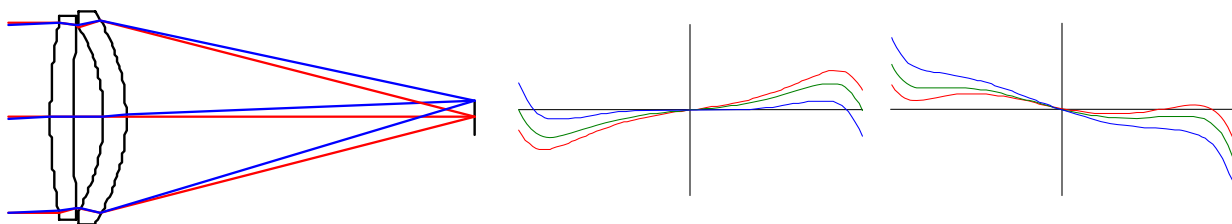
ZnS singlet ($V = 23$)

RMS WFE = .769

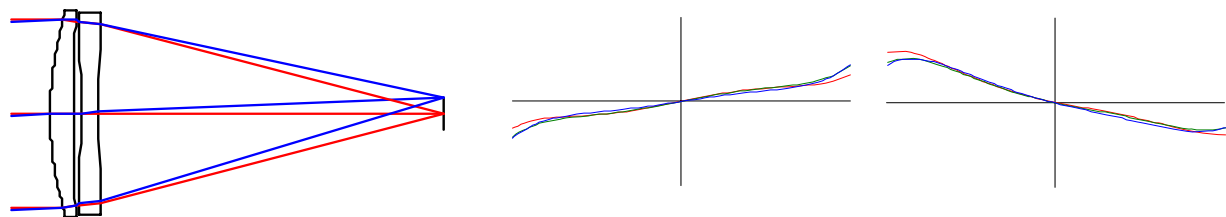
Doublet Design Examples – f/2, 50 mm EFL (8 – 12 μ)



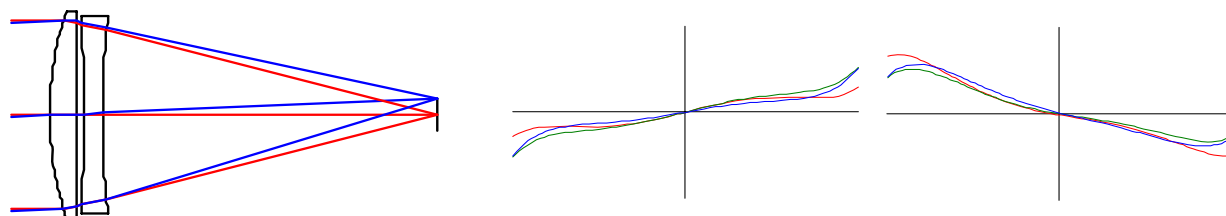
Germanium/ZnS
RMS WFE = .065



Germanium/AMTIR-1
RMS WFE = .064



AMTIR-1/ZnS
RMS WFE = .074



ZnSe/ZnS
RMS WFE = .079

Temperature Effects

- An optical element has two properties which cause changes in optical performance with temperature
 - The **coefficient of thermal expansion**, CTE, usually denoted by α with units of length/length/°C
 - The **change in refractive index with temperature** dn/dT

- The change in focal length of a lens with temperature is given by

$$\Delta F = F \left(\alpha - \frac{1}{n-1} \frac{dn}{dT} \right) \Delta T$$

- Since in most cases the focal length decreases with temperature, the equation is usually stated as $\Delta F = -v F \Delta T$ where

$$v = \frac{1}{n-1} \frac{dn}{dT} - \alpha$$

- v is often referred to as the **thermo-optic coefficient**
- The shift in focus relative to the image plane also includes the CTE of the lens mount, so the shift in focus is given by $\Delta_{\text{focus}} = -(v + \alpha_{\text{mount}}) F \Delta T$

ν Values of Optical Materials ($\times 10^6/^{\circ}\text{C}$)

- Visible glasses

BK7	1.5
BaK4	0.3
BaK50	-11.4
SK16	3.4
SF4	-3.8

It is possible to find combinations of visible glasses to make an athermal design with common mounting materials

- Infrared glasses

Germanium	127
Tl-1173	34
ZnS	28
ZnSe	35
Silicon	63

Most common IR materials have positive ν , so it is more difficult to make a passive athermal design

- CTE of common mount materials ($\times 10^6/^{\circ}\text{C}$)

Aluminum 6061	23.4
416 stainless	9.9
Invar35	0.6
Titanium	8.7
Beryllium	11.6

Example of Temperature Change

- An IR lens is made of germanium for use at 10 microns
- It has a focal length of 4 inches and an aperture of 2 inches (f/2)
- The diffraction-limited depth of focus is $\pm 2\lambda f^2 = \pm 0.0032$ inches
- If we mount the lens in an aluminum mount, the change in focus is $\Delta_{\text{focus}} = 4(-127-23) \times 10^{-6} / ^\circ\text{C} = -0.0006$ in/ $^\circ\text{C}$
- The lens defocus will exceed the diffraction depth of focus over a change in temperature of $\pm 5^\circ\text{C}$
 - Note that for military applications, the operating temperature range is typically $\pm 50^\circ\text{C}$

Making an Athermal Doublet

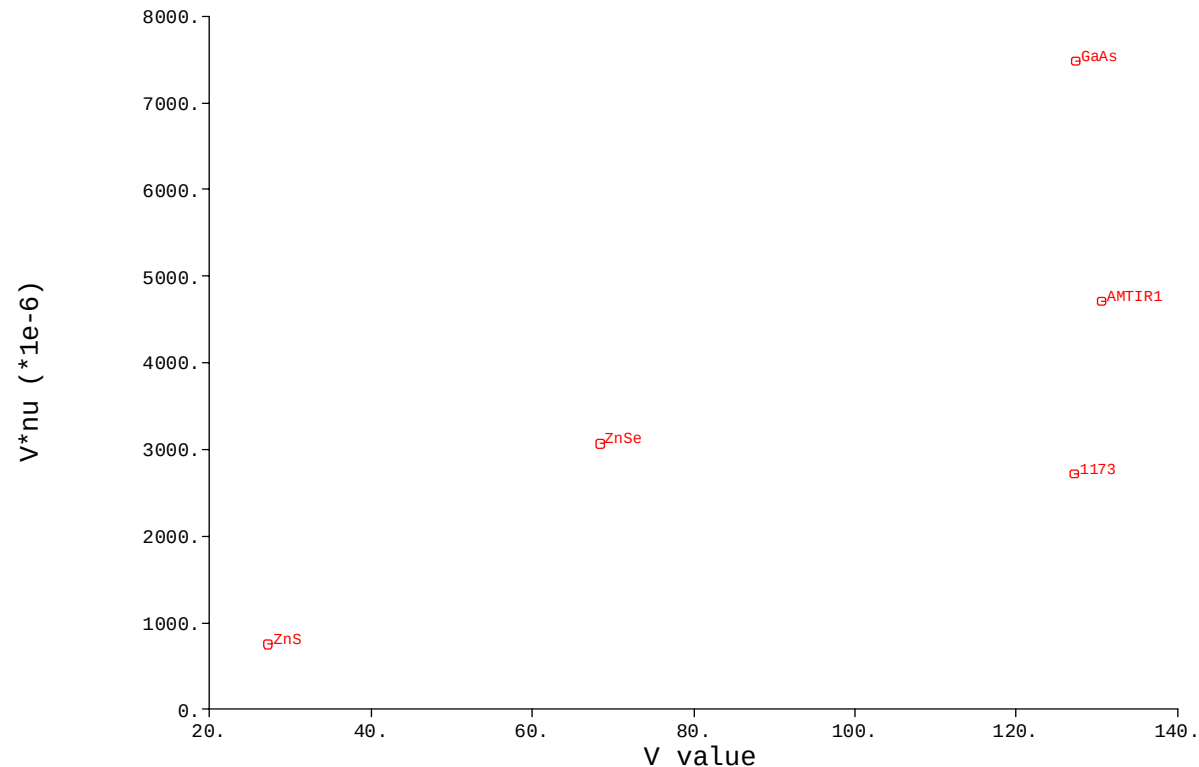
- To satisfy achromatism, the two lenses of a doublet must satisfy the usual achromatic equations

$$f_a = f (V_a - V_b) / V_a$$

$$f_b = f (V_b - V_a) / V_b$$

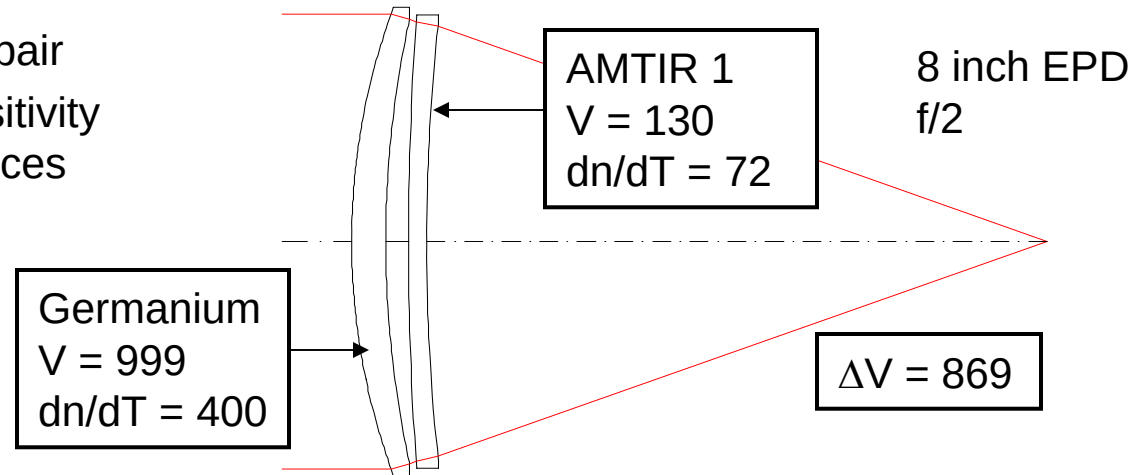
- To be athermalized, the lenses must also satisfy

$$V_a v_a = V_b v_b$$

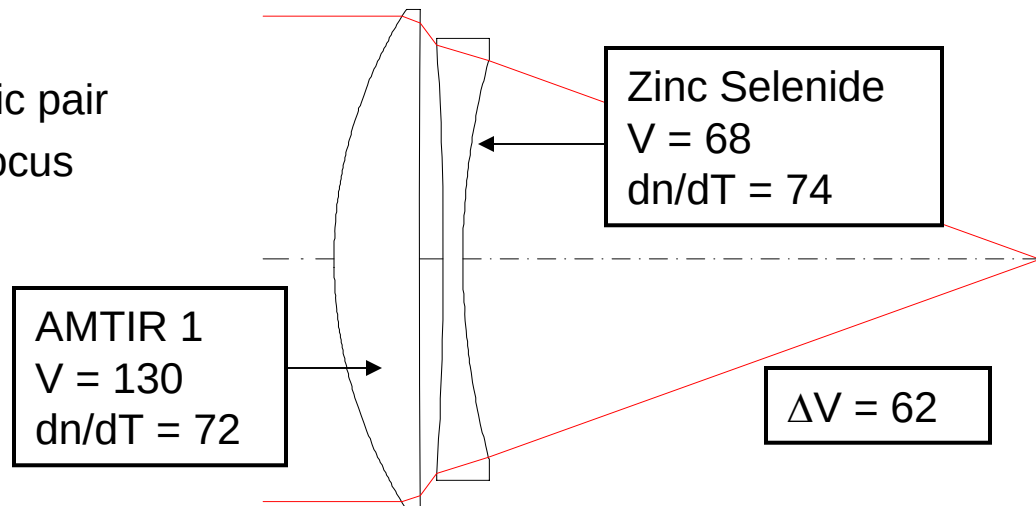


IR Achromatic Doublet Examples (8 - 11.5 microns)

- Common IR achromatic pair
 - Up to 25% less sensitivity to dispersion tolerances



- Reduced dn/dT achromatic pair
 - 3X lower change in focus due to temperature



Infrared Optics Suppliers

- Elcan Optical Systems, Richardson, TX
- Corning NetOptix, Keene, NH
- Exotic Electro-Optics, Marietta, CA
- Optimum Optical Systems, Camarillo, CA
- II-VI Incorporated, Saxonburg, PA
- Janos Technology, Keene, NH
- DRS Optronics, Palm Bay, FL
- Coherent, Auburn, CA
- Diversified Optical Products, Salem, NH
- Telic OSTI, North Billerica, MA

References

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- Optical System Design, Fischer and Tadic-Galeb, McGraw-Hill (2000)
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